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Structural, mechanical, thermodynamic, and electronic properties of thorium hydrides from first-principles

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ABSTRACT

We perform first-principles calculations of the structural, electronic, mechanical, and thermodynamic properties of thorium hydrides (TH_2 and Th_4H_{15}) based on the density functional theory with generalized gradient approximation. The equilibrium geometries, the total and partial densities of states, charge density, elastic constants, elastic moduli, Poisson's ratio, and phonon dispersion curves for these materials are systematically investigated and analyzed in comparison with experiments and previous calculations. These results show that our calculated equilibrium structural parameters are well consistent with experiments. The Th-H bonds in all thorium hydrides exhibit weak covalent character, but the ionic properties for TH_2 and Th_4H_{15} are different due to their different hydrogen concentration. It is found that while in TH_2 about 1.5 electrons transfer from each Th atom to H, in Th_4H_{15} the charge transfer from each Th atom is around 2.1 electrons. Our calculated phonon spectrum for the stable body-centered tetragonal phase of TH_2 accords well with experiments. In addition we show that TH_2 in the fluorite phase is mechanically and dynamically unstable.

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1. Introduction

Thorium is one kind of important nuclear materials and together with its compounds has been widely investigated both experimentally and theoretically. Among thorium compounds, thorium hydrides (ThH₂ and Th₄H₁₅) are metallic solids and have potential use for advanced nuclear fuels. In addition, Th₄H₁₅ has been reported to have superconductivity with transition temperatures $T_c \sim 8$ K [1] and has been considered as promising candidates for hydrogen storage since its large hydrogen-to-metal ratio [2]. ThH₂ is not superconducting above 1 K [3].

Despite the abundant research on thorium hydrides, relatively little is known regarding their chemical bonding, mechanical properties, and phonon dispersion. Only the optical phonon density of states of ThH₂ and Th₄H₁₅ was measured through inelastic neutron scattering [4] and the bulk modulus of ThH₂ was calculated by linear muffin-tin orbital (LMTO) method [5]. Until now the elastic properties, which relate to various fundamental solid-state properties such as interatomic potentials, equation of state, phonon spectra, and thermodynamical properties, are unknown for ThH₂ and Th₄H₁₅. In addition, although the electronic properties as well as the chemical bonding in thorium hydrides have been calculated recently by Shein et al. [2] through the full-potential LAPW (FLAPW) method, the study of the bonding nature of Th–H bond involving its mixed ionic/covalent character is still lacking. These facts, as a consequence, inhibit deep understanding of thorium hydrides. Motivated by these observations, in this paper, we present a first-principles study by calculating the structural, electronic, mechanical, and thermodynamic properties of thorium hydrides. Also, the stability of the metastable phase of ThH₂ (fluorite structure with space group $Fm\bar{3}m$) is analyzed and our calculated results show that the fluorite-type ThH₂ is mechanically unstable. We perform the Bader analysis [6,7] of thorium hydrides and find that about 1.5 (2.1) electrons transfer from each Th atom to H for ThH₂ (Th₄H₁₅).

2. Computational method

Our total energy calculations are carried out by employing the plane-wave basis pseudopotential method as implemented in Vienna *ab initio* simulation package (VASP) [8]. The exchange and correlation effects are described by the density functional theory (DFT) within generalized gradient approximation (GGA) [9]. The projected augmented wave (PAW) method of Blöchl [10] is implemented in VASP with the frozen-core approximation. The thorium $6s^27s^26p^66d^1$ 5f¹ and the hydrogen $1s^1$ electrons are treated as valence electrons. Note that although the 5f states are empty in



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elemental Th, this level turns to evolve into a hybridization with the hydrogen orbitals both in the valence band and the conduction band, as well as to prominently contribute to the conduction band (see Fig. 3 below). $9 \times 9 \times 9$ and $5 \times 5 \times 5$ Monkhorst–Pack [11] *k* point-meshes in the full wedge of the Brillouin zone are used for ThH₂ and Th₄H₁₅, respectively. Electron wave function is expanded in plane waves up to a cutoff energy of 450 eV, and all atoms are fully relaxed until the Hellmann–Feynman forces become less than 0.02 eV/Å.

In present work, the theoretical equilibrium volume, bulk modulus *B*, and pressure derivative of the bulk modulus *B'* are obtained by fitting the energy-volume data in the third-order Birch–Murnaghan equation of state (EOS) [12]. In order to calculate elastic constants, a small strain is applied onto the structure. For small strain ϵ , Hooke's law is valid and the crystal energy $E(V,\epsilon)$ can be expanded as a Taylor series [13],

$$E(V,\epsilon) = E(V_0,0) + V_0 \sum_{i=1}^{6} \sigma_i e_i + \frac{V_0}{2} \sum_{i,j=1}^{6} C_{ij} e_i e_j + O(\{e_i^3\}),$$
(1)

where $E(V_0,0)$ is the energy of the unstrained system with the equilibrium volume $V_{0,\epsilon}$ is strain tensor which has matrix elements $\varepsilon_{i-j}(i,j = 1, 2, \text{ and } 3)$ defined by

$$\varepsilon_{ij} = \begin{pmatrix} e_1 & \frac{1}{2}e_6 & \frac{1}{2}e_5\\ \frac{1}{2}e_6 & e_2 & \frac{1}{2}e_4\\ \frac{1}{2}e_5 & \frac{1}{2}e_4 & e_3 \end{pmatrix}$$
(2)

and C_{ij} are the elastic constants. For cubic structures, there are three independent elastic constants (C_{11} , C_{12} , and C_{44}). So, the elastic constants for fcc ThH₂ and bcc Th₄H₁₅ can be calculated from three different strains listed in the following:

$$\begin{aligned} \epsilon^1 &= (\delta, \delta, \delta, 0, 0, 0), \quad \epsilon^2 &= (\delta, 0, \delta, 0, 0, 0), \quad \epsilon^3 \\ &= (0, 0, 0, \delta, \delta, \delta). \end{aligned}$$
(3)

The strain amplitude δ is varied in steps of 0.006 from $\delta = -0.036$ to 0.036 and the total energies $E(V, \delta)$ at these strain steps are calculated. After obtaining elastic constants, we can calculate bulk and shear moduli from the Voigt–Reuss–Hill (VRH) approximations [14–16]. The Voigt (Reuss) bounds on the bulk modulus B_V (B_R) and shear modulus G_V (G_R) for these two cubic crystal systems are deduced from the formulae of elastic moduli in Ref. [17]. As for bct ThH₂, the six independent elastic constants (C_{11} , C_{12} , C_{44} , C_{13} , C_{33} , and C_{66}) can be obtained from six different strains listed in the following:

$$\begin{aligned} \epsilon^{1} &= (\delta, \delta, \delta, 0, 0, 0), \quad \epsilon^{2} &= (\delta, 0, \delta, 0, 0, 0), \\ \epsilon^{3} &= (\delta, \delta, 0, 0, 0, 0), \quad \epsilon^{4} &= (0, 0, \delta, 0, 0, 0), \\ \epsilon^{5} &= (0, 0, 0, \delta, \delta, 0), \quad \epsilon^{6} &= (0, 0, 0, 0, 0, \delta) \end{aligned}$$
(4)

and the formulae of elastic moduli in VRH approximations [16] are from Ref. [18]. Based on Hill approximation [16], $B = \frac{1}{2}(B_R + B_V)$ and $G = \frac{1}{2}(G_R + G_V)$. The Young's modulus *E* and Poisson's ratio v are given by the following formulae:

$$E = 9BG/(3B+G), \quad v = (3B-2G)/[2(3B+G)].$$
(5)

3. Results

3.1. Atomic and electronic structures of thorium hydrides

At ambient condition, the stable thorium dihydride crystallizes in a body-centered tetragonal (bct) ionic structure with space group I4/mmm (No. 139). Its unit cell is composed of two ThH₂ formula units with the thorium atoms and the hydrogen atoms in 2*a* (in Wyckoff notation) and 4*d* sites, respectively (see Fig. 1a). Each Th atom is surrounded by eight H atoms forming a tetragonal and each H connects with four Th atoms to build a tetrahedron. The present optimized lattice parameters (a and c) are 4.0670 Å and 4.9125 Å (see Table 1), in good agreement with the experimental [19] values of 4.10 Å and 5.03 Å. Besides, the face-centered cubic (fcc) fluorite-type structure with space group $Fm\bar{3}m$ (No. 225) is considered as metastable phase for ThH₂ (see Fig. 1b). The fluorite structure is the stable structure of all actinide dioxides. Moreover, this fcc structure can be obtained from the bct stable structure by modulating the base vectors. In fcc structure, each Th atom is surrounded by eight H atoms forming a cube and each H connects with four Th atoms to build a tetrahedron. Our optimized lattice constant (a) for fcc ThH₂ is 5.4851 Å (see Table 1), in excellent agreement with the measured [5] values of 5.489 Å. The structure of Th₄H₁₅ is more complicated. It crystallizes in a body-centered cubic (bcc) structure with space group $I\bar{4}3d$ (No. 220) (see Fig. 1c). The unit cell has 16 Th (16c). 12 H1 (12a). and 48 H2 (48e) atoms. Each H1 is surrounded by four Th atoms to build the tetrahedral structure and each H2 is located at the center of triangle formed by three Th atoms. As a result, each Th is surrounded by three H1 atoms and nine H2 atoms. In Fig. 1c, we label clearly the H1 atoms (red spheres) and H2 atoms (grey spheres) connected to the Th atom located at center. The current optimized structural parameters of Th₄H₁₅ are listed in Table 1, where one can find that our calculation results are in good agreement with experiment [20].

To investigate the stability of ThH₂, we have optimized the structural parameters of its bct and fcc structures at different pressures. To avoid the Pulay stress problem, we perform the structure relaxation calculations at fixed volumes rather than constant pressures. For fcc structure, due to its high symmetry, the structure relaxation calculations are performed at fixed volumes with no relaxation of coordinates and cell shape. However, for bct structure, the cell shape is necessary to be optimized due to their internal degrees of freedom. The total energies (per primitive cell) of the two structures at different volumes are calculated and shown in Fig. 2. Obviously, the bct ThH₂ is more stable than fcc ThH₂ under ambient pressure. The equilibrium volumes of bct and fcc structures are 40.63 Å³ and 41.26 Å³, respectively. Thus the equilibrium volumes of both bct and fcc phases are approximately equal and the total energy difference at their equilibrium states is \sim 0.032 eV. This conclusion is consistent well with the previous FLAPW results [2].

Basically, all the macroscopical properties of materials, such as hardness, elasticity, and conductivity, originate from their electronic structure properties as well as chemical bonding nature. Therefore, it is necessary to perform the electronic structure analysis of thorium hydrides. The calculated total densities of states (DOS) and the orbital-resolved partial densities of states (PDOS) of bct ThH₂, fcc ThH₂ and bcc Th₄H₁₅ are shown in Fig. 3. Overall, the occupation properties of ThH₂ in bct and fcc phases are similar. The occupied DOS near the Fermi level is featured by the three well-resolved peaks. The one near -1.0 eV is principally Th 6d in character, while the other two peaks respectively near -4.5 and -6.0 eV are mostly H 1s hybridized with Th 6d and Th 5f orbitals. These well-separated orbital peaks have been observed in the photoelectron spectroscopy (PES) measurement [21]. In addition, the band width of the Th 6d valence band near the Fermi level is 3 eV, consistent with the FLAPW calculation [2] and experimental data [21]. The H 1s valence band width is of 5.0 eV, also in accord with the experimental data (6.0 eV) and previous FLAPW result (5.2 eV). Moreover, the low bands of bct (fcc) ThH₂ covering from -18.8 (-19.0) to -17.2 (-17.5) eV is mainly featured by Th 6p state mixed with a little H 1s state and the conduction bands is principally occupied by Th 5f states with admixtures of the Th 6d and H 1s states and has a width of 5.5 (5.1) eV. For Th_4H_{15} , our



Fig. 1. Crystal structures of (a) bct ThH₂, (b) fcc ThH₂, and (c) bcc Th₄H₁₅. Here, larger cyan spheres stand for Th atoms and the smaller white H. Note that the magenta and red spheres in (c) stand for H1 and the white and grey spheres H2. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Table 1

Optimized structural parameters, partial and total densities of states at the Feimi level $N(E_F)$ states/eV/Th atom for thorium hydrides. For comparison, other theoretical results mid available experimental data are also listed.

Compound	Cell constants (Å)	Coordinates	Th 6 <i>d</i>	Th 5 <i>f</i>	H s	Total
bct ThH ₂ ($I4/mmm$) fcc ThH ₂ ($Fm\bar{3}m$) Th ₄ H ₁₅ ($I\bar{4}3d$)	$a = 4.0670 (4.0475)^{a}, (4.10)^{c}$ $c = 4.9125 (4.9778)^{a}, (5.03)^{c}$ $a = 5.4851 (5.4902)^{a}, (5.489)^{b}$ $a = 9.1304 (9.1280)^{a}, (9.11)^{c,d}$	Th (2 <i>a</i>): 0,0,0 H (4 <i>d</i>): 0, 0.5, 0.25 Th (4 <i>a</i>):0, 0,0 H (8 <i>c</i>): 0.25, 0.25, 0.25 Th (16 <i>c</i>): <i>x</i> , <i>x</i> , <i>x</i> : <i>x</i> = 0.2087 (0.208) ^d H1 (12 <i>a</i>): 0.375, 0, 0.25 H2 (48 <i>e</i>): 0.372, 0.219, 0.404 (0.4, 0.23, 0.372) ^d	$\begin{array}{c} 0.383 \\ (0.207)^{a} \\ 0.610 \\ (0.374)^{a} \\ 0.610 \\ (0.441)^{a} \end{array}$	$\begin{array}{c} 0.165 \\ (0.140)^{a} \\ 0.244 \\ (0.202)^{a} \\ 0.678 \\ (0.619)^{a} \end{array}$	$\begin{array}{c} 0.002 \\ (0.001)^a \\ 0.003 \\ (0.002)^a \\ 0.031 \\ (0.049)^a \end{array}$	$\begin{array}{c} 0.996 \\ (0.866)^a \\ 1.557 \\ (1.451)^a \\ 2.334 \\ (2.474)^a \end{array}$

^a Ref. [2].

^b Ref. [5].

^c Ref. [19].

^d Ref. [20].



Fig. 2. Comparison of total energy vs. the primitive cell volume for ThH_{2} in bct and fcc phases.

calculations reproduce all the features calculated by Shein et al. [2] and agree well with PES measurements [21]. Note that our calculated conduction band width is 1.7 eV, consistent with the PES experimental value [21] (0.9 eV) and evidently smaller than that of FLAPW calculation result [2]. The main occupation of conduction

bands is Th 5*f* orbital, mixed with a little Th 6*d* and H 1*s* states. In addition, we have also presented in Table 1 the partial and total DOSs at the Feimi level $N(E_F)$ for thorium hydrides to study the occupation of the conduction band. Clearly, our results are in good agreement with the FLAPW calculation [2].

In order to gain more insight into the bonding nature of ground state thorium hydrides, we also investigate the valence charge density distribution. The calculated valence charge density maps of the bct ThH₂ in (100) plane, fcc ThH₂ in ($1\overline{1}0$) plane, and bcc Th₄H₁₅ in plane established by three Th and one H2 atoms are plotted in Fig. 4. Clearly, the charge densities around Th and H ions are all near spherical distribution with slightly deformed towards the direction to their nearest neighboring atoms. To describe the ionic/covalent character quantitatively and more clearly, we plot in Fig. 5 the line charge density distribution along the nearest Th-H bonds and perform the Bader analysis [6,7]. For bct and fcc ThH₂, the two charge density curves change with the same way along the Th–H bonds. For Th₄H₁₅, the two curves along the Th–H1 and Th-H2 bonds are almost the same before the bridge locus (indicated by the arrow), after where they split evidently. Besides, one can find a minimum value of charge density in Fig. 5 for each bond at around the bridge. These minimum values are listed in Table 2. Although these values are much smaller than $0.7 \text{ e/}\text{Å}^3$ for Si covalent bond, they are prominently higher than $0.05 \text{ e/}\text{Å}^3$



Fig. 3. Total and orbital-resolved local densities of states for (a) bct ThH₂, (b) fcc ThH₂, and (c) bcc Th₄H₁₅. The Fermi energy level is set at zero.



Fig. 4. Valence charge density of (a) bct ThH₂ in (100) plane, (b) fcc ThH₂ in (1 $\overline{1}$ 0) plane, and (c) bcc Th₄H₁₅ in plane established by three Th and one H2 atoms. Contour lines are drawn from 0.0 to 1.0 at 0.05 e/Å³ intervals.



Fig. 5. Line charge density distribution between Th atom and the nearest neighbor H atom for bct ThH_2 , fcc ThH_2 , and bcc Th_4H_{15} .

for Na-Cl bond in typical ionic crystal NaCl. Also we notice that these values are smaller than the minimum values $(0.45 \text{ e}/\text{\AA}^3)$ of charge density along the Th-O bond in our previous study of ThO₂ [22]. Therefore, there are weak but clear covalent bonds between Th and H for ThH₂ in bct and fcc phases and for bcc Th₄H₁₅. The slight difference appears in Th₄H₁₅, where the minimum value of charge density in Th-H1 bond is smaller than that in Th-H2 bond. In addition, one can notice from Table 2 that our calculated Th-H distances are all well consistent with the previous theoretical [5] and experimental [19] results. As for Bader analysis, it is a well established analysis tool for studying the topology of the electron density and thus is particularly suitable for discussing the mixed ionic/covalent character of a compound. The charge (Q_B) enclosed within the Bader volume (V_R) is a good approximation to the total electronic charge of an atom. In the present study, the default charge density grids for one unit cell are $56 \times 56 \times 72$, $56 \times 56 \times 56,$ and $112 \times 112 \times 112$ for bct ThH_2, fcc ThH_2, and bcc Th₄H₁₅, respectively. To check the precision, the charge density distribution for fcc ThH₂ is calculated with a series of n times finer grids (n = 2, 3, 4, 5, 6). The deviation of the effective charge

Table 2

Calculated charges and volumes according to Bader partitioning as well as the Th-H distances and correlated minimum values of charge densities along the Th-H bonds for thorium hydrides. As a comparison, other theoretical work and available experimental data are also listed. Note that some properties of Th_4H_{15} have two values (first for H1 and second for H2).

Compound	$Q_B(Th)(e)$	$Q_B(H)(e)$	$V_B(Th)$ (Å ³)	$V_B(H)$ (Å ³)	Th-H (Å)	Charge density _{min} (e/Å ³)
bct ThH ₂	10.530	1.735	25.59	7.50	$\begin{array}{l} 2.375~(2.385)^{a}\\ 2.375~(2.337)^{b}\\ 2.465~(2.46)^{a},~2.343~(2.29)^{a} \end{array}$	0.273
fcc ThH ₂	10.488	1.756	25.72	7.77		0.271
Th ₄ H ₁₅	9.870	1.590, 1.563	20.15	7.16 , 7.35		0.231, 0.296

^a Ref. [19].

in Th₄H₁₅ are more ionized than that in thorium dihydrides.

3.2. Mechanical properties of thorium hydrides

Our calculated elastic constants, various moduli, pressure derivative of the bulk modulus B', and Poisson's ratio v for bct ThH₂, fcc ThH₂, and bcc Th₄H₁₅ are collected in Table 3. Obviously, bct ThH₂ is mechanically stable due to the fact that its elastic constants satisfy the following mechanical stability criteria [23] of tetragonal structure:

$$\begin{aligned} & \mathcal{C}_{11} > 0, \quad \mathcal{C}_{33} > 0, \quad \mathcal{C}_{44} > 0, \quad \mathcal{C}_{66} > 0, \\ & (\mathcal{C}_{11} - \mathcal{C}_{12}) > 0, \quad (\mathcal{C}_{11} + \mathcal{C}_{33} - 2\mathcal{C}_{13}) > 0, \\ & [2(\mathcal{C}_{11} + \mathcal{C}_{12}) + \mathcal{C}_{33} + 4\mathcal{C}_{13}] > 0. \end{aligned}$$

 Th_4H_{15} is also mechanically stable because its elastic constants satisfy the following mechanical stability criteria [23] of cubic structure:

$$C_{11} > 0, \quad C_{44} > 0, \quad C_{11} > |C_{12}|, \quad (C_{11} + 2C_{12}) > 0.$$
 (7)

However, the ThH₂ in its metastable cubic phase is mechanically unstable. In fact, one can see from Table 3 that C_{11} is much smaller than C_{12} for fcc ThH₂. Therefore, the mechanical stability criteria [23] $C_{11} > |C_{12}|$ can not be satisfied and the shear modulus, Young's modulus, and Poisson's ratio also can not be obtained. As for bulk modulus *B*, each derived value from VRH approximations [16] for all the thorium hydrides turns out to be very close to that obtained by EOS fitting. Moreover, we notice that our calculated *B* for fcc ThH₂ is approximately equal to previous LMTO theoretical result [5]. For shear modulus *G* and Young's modulus *E*, their values for bcc Th₄H₁₅ are approximately 2.5 times of those for bct ThH₂. For Poisson's ratio, the values for both bct ThH₂ and bcc Th₄H₁₅ are within the range from 0.25 to 0.45 for typical metals.

3.3. Phonon dispersion curves of thorium dihydrides

Employing the Hellmann–Feynman theorem and the direct method [24], we have calculated the phonon curves along some high-symmetry directions in the Brillouin zone (BZ), together with the phonon PDOS. For the phonon dispersion calculation, we use the $2 \times 2 \times 2$ bct (fcc) supercell containing 48 (96) atoms for bct (fcc) ThH₂. To calculate the Hellmann–Feynman forces, we displace four and eight atoms, respectively, for bct and fcc ThH₂ from their equilibrium positions and the amplitude of all the displacements is 0.03 Å. The calculated phonon dispersion curves along the $\Gamma - N - P - X - \Gamma - Z$ directions for bct ThH₂ and along the $\Gamma - X - K - \Gamma - L - X - W - L$ directions for fcc ThH₂ are displayed in Fig. 6a and b, respectively.

For both bct and fcc ThH₂, there are only three atoms in their primitive cells. Therefore, nine phonon modes exist in the dispersion relations. Due to the fact that thorium is much heavier than hydrogen atom, the vibration frequency of thorium atom is apparently lower than that of hydrogen atom. Therefore, evident gap between the optic modes and the acoustic branches exits and the phonon DOS of bct (fcc) ThH₂ can be viewed as two parts. One is the part lower than 4.4 (4.1) THz where the main contribution comes from the thorium sublattice, while the other part range from 26.0 to 32.1 (26.4 to 31.8) THz is dominated by the dynamics of the light hydrogen atoms. In experimental measurements, Dietrich et al. reported that the acoustic branches of ThH₂ are lower than 4.8 THz and optic modes range from 23.4 to 36.2 THz [4]. Their measured data of optic modes are presented in Fig. 6a for comparison and the acoustic-phonon data are unable obtained from their time-of-flight spectrum. Obviously, our calculated results are on the whole consistent with the experimental data. In addition, all frequencies are positive for bct ThH₂, which assures a dynamical stability of the bct phase against mechanical perturbations. However, for fcc ThH₂, one can see from Fig. 6b that the transverse acoustic (TA) mode close to Γ point becomes imaginary along the $\Gamma - K$ and $\Gamma - L$ directions. The minimum of the TA branch occurs along the $\Gamma - K$ direction. This indicates instability of fcc phase of ThH₂ compared to stable bct phase, which is well consistent with our previous mechanical stability analysis of ThH₂.

Table 3											
Calculated	elastic	constants.	various	moduli.	and	Poisson's	ratio	v for	thorium	livdrid	les

Compound	<i>C</i> ₁₁ (GPa)	<i>C</i> ₁₂ (GPa)	C ₄₄ (GPa)	C ₁₃ (GPa)	C ₃₃ (GPa)	C ₆₆ (GPa)	B (GPa)	<i>B</i> ′ (GPa)	G (GPa)	E (GPa)	ν
bct ThH ₂	131	100	29	78	89	5	91	3.3	16	44	0.419
fcc ThH ₂	46	119	57				95 (99) ^a	3.8			
Th ₄ H ₁₅	121	66	59				85	2.2	43	111	0.282

^b Ref. [5].

between the five and the six times finer grids is less than 0.02%. Thus we perform the charge density calculations using the six times finer grid ($336 \times 336 \times 432$, $336 \times 336 \times 336$, and $672 \times$ 672×672 for bct ThH₂, fcc ThH₂, and bcc Th₄H₁₅, respectively). The calculated results are presented in Table 2. Note that although we have included the core charge in charge density calculations, since we do not expect variations as far as the trends are concerned, only the valence charge are listed. From Table 2 the following prominent features can be seen: (i) The Bader charges and volumes for bct and fcc ThH₂ are almost equal to each other. This shows the same ionic character, through a flux of charge (about 1.5 electrons for each Th atom) from cations towards anions, for thorium dihydride both in their stable phase and metastable phase. (ii) The Bader charges and volumes for bcc Th₄H₁₅ are different comparing to thorium dihydride. This originates from their different hydrogen concentration. For bcc Th₄H₁₅, about 2.1 electrons transfer from each Th atom to H. This indicates that the Th atoms



Fig. 6. Calculated phonon dispersion curves and corresponding PDOS for (a) bct ThH₂ and (b) fcc ThH₂. For comparison, the experimental data in Ref. [4] are also shown (squares).

Moreover, there exists LO-TO splitting at Γ point in bct phase. But in fcc phase there is no LO-TO splitting.

4. Conclusion

In summary, we have used the first-principles DFT-GGA method to calculate the structural, electronic, mechanical, and thermodynamic properties of ThH₂ in its stable bct phase and metastable fcc phase and Th₄H₁₅ in bcc phase. Our optimized structural parameters are well consistent with experiments. The occupation characters of electronic orbitals also accord well with experiments and previous calculations. Through Bader analysis, we have found that the Th–H bonds in all thorium hydrides exhibit weak covalent character, but the ionic property for ThH₂ and Th₄H₁₅ are different. While ~1.5 electrons transfer from each Th atom to H in ThH₂, in Th₄H₁₅ about 2.1 electrons deviate from each Th atom. In addition, our calculated phonon curves of fcc ThH₂ have shown that the TA mode becomes imaginary close to Γ point and the subsequent instability of this phase.

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